

## Department of Mathematics Johns Hopkins University

# 110.413 Introduction to Topology Course Syllabus

The following list of topics is considered the core content for the course 110.413 Introduction to Topology. The current text for the course is:

Text: <u>Topology</u>, 2<sup>nd</sup> Ed., Munkres, J., New Jersey: Prentice Hall, January, 2000, ISBN-10: 0131816292, ISBN-13: 978-0131816299.

### **Course Topics**

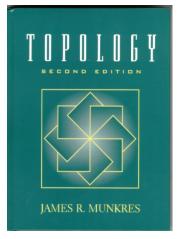
- General Topology
  - Set Theory and Logic (1+ weeks)
    - 1 Fundamental Concepts
    - 2 Functions
    - 3 Relations
    - 4 The Integers and the Real Numbers
    - 5 Cartesian Products
    - 6 Finite Sets
    - 7 Countable and Uncountable Sets
    - 8 The Principle of Recursive Definition
    - 9 Infinite Sets and the Axiom of Choice
    - 10 Well-Ordered Sets
    - 11 The Maximum Principle

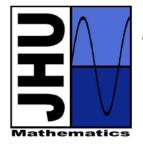
### • Topological Spaces and Continuous Functions (3 weeks)

- 12 Topological Spaces
- 13 Basis for a Topology
- 14 The Order Topology
- 15 The Product Topology on  $X \times Y$
- 16 The Subspace Topology
- 17 Closed Sets and Limit Points
- 18 Continuous Functions
- 19 The Product Topology
- 20-1 The Metric Topology
- 22 The Quotient Topology

### • Connectedness and Compactness (2 weeks)

- 23 Connected Spaces
- 24 Connected Subspaces of the Real Line
- 25 Components and Local Connectedness
- 26 Compact Spaces
- 27 Compact Subspaces of the Real Line
- 28 Limit Point Compactness
- 29 Local Compactness





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### Countability and Separation Axioms (2 weeks)

- 30 The Countability Axioms
- 31 The Separation Axioms
- 32 Normal Spaces
- 33 The Urysohn Lemma
- 34 The Urysohn Metrization Theorem
- 35 The Tietze Extension Theorem
- 36 Imbeddings of Manifolds

### • Algebraic Topology

#### • The Fundamental Group (3 weeks)

- 51 Homotopy of Paths
- 52 The Fundamental Group
- 53 Covering Spaces
- 54 Fundamental Group of a Circle
- 55 Retractions and Fixed Points
- 56 (optional) The Fundamental Theorem of Algebra
- 57 The Borsuk-Ulam Theorem
- 58 Deformation Retracts and Homotopy Type
- 59 The Fundamental Group of  $S^n$
- 60 The Fundamental Group of Some Surfaces

### • (optional) Classification of Surfaces (1 week)

- 74 Fundamental Groups of Surfaces
- 75 Homology of Surfaces
- 76 Cutting and Pasting
- 77 The Classification Theorem
- 78 Constructing Compact Surfaces

#### • Classification of Covering Spaces (1 week)

- 79 Equivalence of Covering Spaces
- 80 The Universal Covering Space
- 81 Covering Transformations
- 82 Existence of Covering Spaces