

Department of Mathematics Johns Hopkins University

# AS.110.202 Calculus III Course Syllabus

The following list of topics is considered the core content for the course AS.110.202 Calculus III. The current text for the course is:

**Text:** <u>Vector Calculus</u>, 6<sup>th</sup> Edition, Marsden, J., and Tromba, A., W.H. Freeman, August 2003, **ISBN-13: 9781429215084, ISBN-10: 1429215089**.

# Course Topics

#### • The Geometry of Euclidean Space (1 week)

- o 1.1 Vectors in Two- and Three-Dimensional Space
- o 1.2 The Inner Product, Length, and Distance
- o 1.3 Matrices, Determinants, and the Cross Product
- o 1.4 Cylindrical and Spherical Coordinates
- 1.5 *n*-Dimensional Euclidean Space

# • Differentiation Space (2 weeks)

- 2.1 The Geometry of Real-Valued Functions
- 2.2 Limits and Continuity
- o 2.3 Differentiation
- o 2.4 Introduction to Paths
- 2.5 Properties of the Derivative
- 2.6 Gradients and Directional Derivatives

# • Higher-Order Derivatives: Maxima and Minima (2- weeks)

- 3.1 Iterated Partial Derivatives
- o 3.2 Taylor's Theorem
- 3.3 Extrema of Real-Valued Functions
- o 3.4 Constrained Extrema and Lagrange Multipliers
- 3.5 The Implicit Function Theorem

#### • Vector-Valued Functions (1+ weeks)

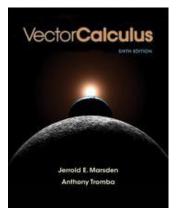
- 4.1 Acceleration and Newton's Second Law
- o 4.2 Arc Length
- o 4.3 Vector Fields
- o 4.4 Divergence and Curl

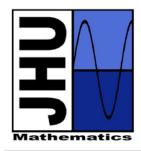
#### • Double and Triple Integrals (1 week)

- o 5.1 Introduction
- 5.2 The Double Integral Over a Rectangle
- o 5.3 The Double Integral Over More General Regions
- 5.4 Changing the Order of Integration
- 5.5 The Triple Integral

# • The Change of Variables Formula and Applications of Integration (1 week)

- $\circ \quad \ \ 6.1 \ The \ Geometry \ of \ Maps \ from \ R^2 \ to \ R^2$
- 6.2 The Change of Variables Theorem





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# • Integrals (2 weeks)

- 7.1 The Path Integral
- 7.2 Line Integrals
- o 7.3 Parameterized Surfaces
- o 7.4 Area of a Surface
- 7.5 Integrals of Scalar Functions Over Surfaces
- 7.6 Surface Integrals of Vector Functions

#### • The Integral Theorems of Vector Analysis (2 weeks)

- 8.1 Green's Theorem
- o 8.2 Stokes' Theorem
- o 8.3 Conservative Fields
- o 8.4 Gauss' Theorem